



Sheet (2)

1. Estimate the directivity of an antenna with $\Theta_{HP} = 2^\circ$ and $\Phi_{HP} = 1^\circ$.
2. Find the number of square degrees in the solid angle Ω on a spherical surface that is between ($\theta = 20^\circ$ and $\theta = 40^\circ$), and ($\phi = 30^\circ$ and $\phi = 70^\circ$).
3. The normalized field pattern of an antenna is given by $E(\theta) = \sin\theta \sin\phi$. E_n has a value only for $0 \leq \theta \leq \pi$ & $0 \leq \phi \leq \pi$, and zero elsewhere, Find
 - a. The exact directivity.
 - b. The approximate directivity.
 - c. The decibel difference.

4. Calculate the D_{approx} from the HPBW of a unidirectional antenna if the power pattern is given by :

$$E(\theta, \phi) = 30 \cos^2\theta \sin^{3/2}\phi$$

$$0 \leq \theta \leq \pi \quad 0 \leq \phi \leq \pi \quad \text{and zero otherwise.}$$

Then repeat by calculating D_{exact} for the previous pattern. Finally calculate the db difference between the exact and approximate records.

5. The far-zone electric-field intensity (array factor) of an end-fire two-element array antenna, placed along the z-axis and radiating into free-space, is given by

$$E = \cos \left[\frac{\pi}{4} (\cos \theta - 1) \right] \frac{e^{-jkr}}{r}, \quad 0 \leq \theta \leq \pi$$

Find the directivity using Kraus' approximate formula

6. The normalized far-zone field pattern of an antenna is given by

$$E = \begin{cases} (\sin \theta \cos^2 \phi)^{1/2} & 0 \leq \theta \leq \pi \text{ and } 0 \leq \phi \leq \pi/2, 3\pi/2 \leq \phi \leq 2\pi \\ 0 & \text{elsewhere} \end{cases}$$

Find the directivity using

- (a) The exact expression
- (b) Kraus' approximate formula

7. Estimate the directivity for a source with relative field pattern
 - a. $E = \cos 2\theta \cos \theta$. Assume a unidirectional pattern.
 - b. $E = \sin\left(\frac{\pi}{2} \cos \theta\right)$. Assume $0 \leq \theta \leq \pi$ & $0 \leq \phi \leq 2\pi$.

Good Luck

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